

## Dynamical properties of defects in diamond

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### Introduction

First, we compute the theoretical Raman spectra of various diamond polymorphs to help provide a quick, non-destructive method of determining planar defects in diamonds.

For this, we use density functional perturbation theory and compute the Raman spectra with peak position and intensity [1-5]. In density functional perturbation theory, the electronic energy  $F$  of an atomic ensemble is expanded as a Taylor series around the equilibrium position of the atoms, with respect to a series of perturbations  $\lambda$  acting along directions  $i, j, k \dots$ :

$$F_{e+i}[\lambda] = F_{e+i}^{(0)}[\lambda] + \sum_i \left( \frac{\partial F_{e+i}}{\partial \lambda_i} \right) \lambda_i + \frac{1}{2} \sum_{ij} \left( \frac{\partial^2 F_{e+i}}{\partial \lambda_i \partial \lambda_j} \right) \lambda_i \lambda_j + \frac{1}{6} \sum_{ij} \left( \frac{\partial^3 F_{e+i}}{\partial \lambda_i \partial \lambda_j \partial \lambda_k} \right) \lambda_i \lambda_j \lambda_k + \dots$$

The Raman spectra involve atomic displacements and electric fields as perturbations. The Raman tensor,  $\alpha$ , determines the intensity of the Raman spectra. Its components are obtained as:

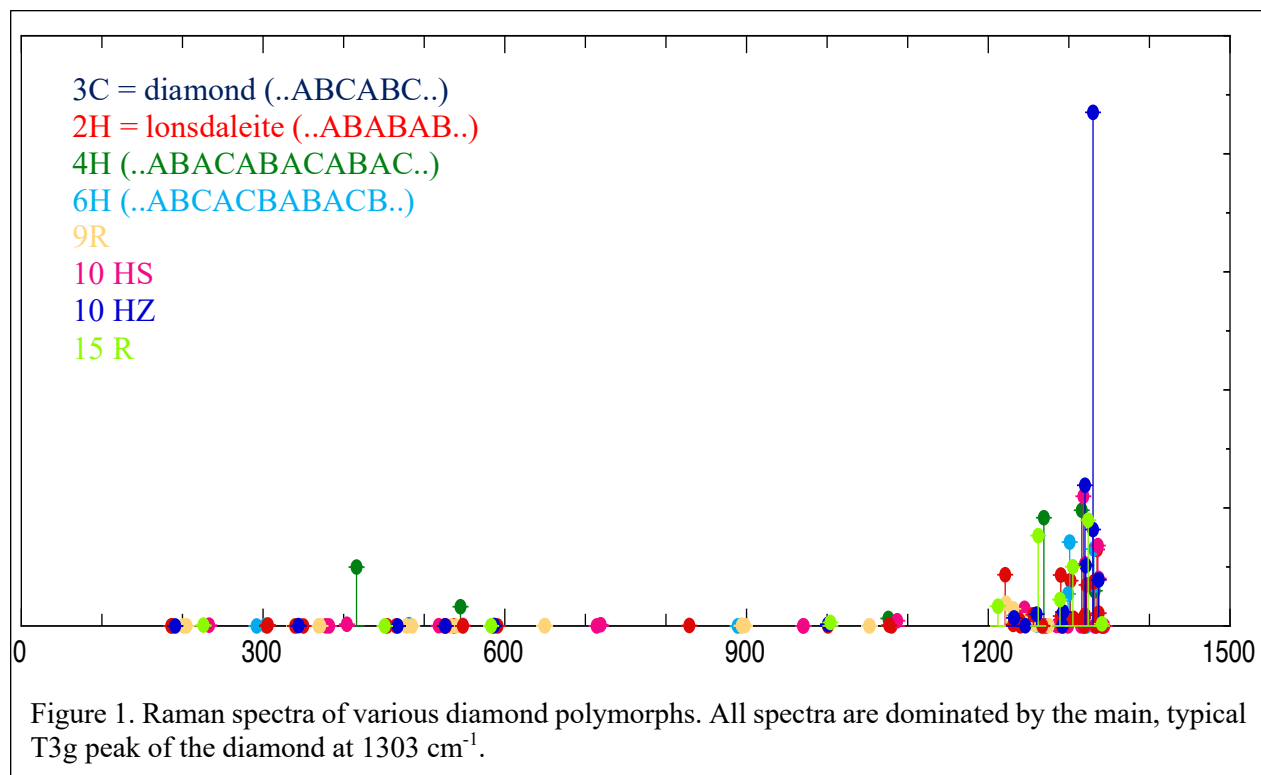
$$\alpha_{ij}^m = \sqrt{\Omega_0} \sum_{\kappa\beta} \frac{\partial \chi_{ij}^{\infty(1)}}{\partial \tau_{\kappa\beta}} \eta_m(\kappa\beta) = \sqrt{\Omega_0} \sum_{\kappa\beta} \frac{\partial}{\partial \tau_{\kappa\beta}} \left( \frac{\partial^2 E}{\partial \mathcal{E}_i \partial \mathcal{E}_j} \right) \mathcal{E}_i \mathcal{E}_j \eta_m(\kappa\beta)$$

where  $\tau$  are displacements of atoms  $\beta$  along directions  $\kappa$ ,  $\chi$  is the dielectric tensor,  $i, j, m$  are cartesian directions, and  $\mathcal{E}$  are electric fields.

Here, we use the ABINIT implementation of the DFPT. Simulations are performed using the Local Density Approximation for the exchange-correlation factor. Results are reported in Figure 1. All the details of the simulations, as well as the raw spectra, can be found on the WURM website [6]. Most of the diamond polytypes are hexagonal; they are all obtained from a different packing sequence. Their occurrence in natural or synthetic diamonds may result as growth defects [7].

All the spectra are dominated by the characteristic T3g peak of diamond at 1303  $\text{cm}^{-1}$ . Note that the theoretical spectrum was realized using an 8x8x8 grid of special  $k$  points; this ensured an error of only 1  $\text{cm}^{-1}$  with respect to experimental data. The spectra were obtained at the experimental density, the slightest change in volume greatly affecting the position of the peaks [8].

While it is hard to distinguish between various individual hexagonal polytypes, their presence can be observed by the appearance of extra peaks and shoulders [9]. The main characteristic of the other polytypes, except for the pure 3C diamond, is the presence of various smaller shoulder peaks in the 1200 – 1300  $\text{cm}^{-1}$  range. As the succession of  $\text{sp}^3$  bonds of carbon is interrupted, the symmetry is broken, resulting in the activation of certain phonons observed in the new Brillouin zones. Further supplementary peaks may occur at low frequency, in the 300 – 600  $\text{cm}^{-1}$  range.



In a second set of simulations, I study the diffusion of Helium in diamond. For this, we employ molecular dynamics (MD) simulations in the Vienna Ab Initio Simulation package [10,11]. I use density functional theory to generate a series of reference structures and MD trajectories. Then, I use machine learning techniques to fit interatomic potentials on the ab initio data. To ensure the quality of the potentials and to avoid unphysical structures, I also generate a series of configurations characterized by very large interatomic forces and high energies. As I study the diffusion of He in diamond along a mantle adiabat, I refine the machine learning potentials at each pressure.

With the machine-learning potentials, I use large simulation boxes with 1728 atoms, corresponding to 6x6x6 supercells of the conventional Fm3m unit cell of diamond, in which I randomly insert one He atom. The simulations are run with a time step of 0.5 femtosecond. After a thermalization period of 1000 steps, the simulations record a production length of 400 to 600 picoseconds. I employ the Universal Molecular Dynamics package [12] to perform the post-processing analysis of the MD runs.

I report the diffusion coefficients as a function of pressure and temperature, following the mantle geotherm. I find that temperature is the major factor ruling the diffusion coefficients of He in diamonds.

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